

## Lesson 20: Solving Inequalities

An **inequality** is a mathematical sentence comparing two expressions that are not equal. An inequality may use one of the following symbols:  $<$  or  $>$ . The symbol  $>$  means “is greater than.” The symbol  $<$  means “is less than.”

To solve inequalities, follow the same rules as for solving equations. Use inverse operations to isolate the variable.

### Example

Solve the following inequality for  $x$ .

$$5x < -35$$

Use inverse operations to solve for  $x$ .

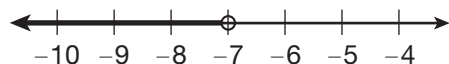
$$5x < -35$$

$$\frac{5x}{5} < -\frac{35}{5} \quad \text{Divide both sides by 5.}$$

$$x < -7$$

The solution set for the inequality is  $x < -7$ .

The graph of the solution set is shown below.



Notice that the dot on  $-7$  is open. This means that  $-7$  is not included as part of the solution set.

To check the answer, substitute any number less than  $-7$  for  $x$ . Use  $x = -8$ .

$$5x < -35$$

$$5(-8) < -35$$

$$-40 < -35$$

### ▶ Example

Solve the following inequality for  $x$ .

$$8 + x \geq 5$$

Use inverse operations to solve for  $x$ .

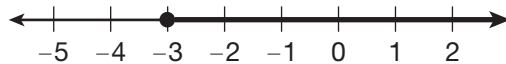
$$8 + x \geq 5$$

$$8 - 8 + x \geq 5 - 8 \quad \text{Subtract 8 from both sides.}$$

$$x \geq -3$$

The solution set for the inequality is  $x \geq -3$ .

The graph of the solution set is shown below.



Notice that the dot on  $-3$  is filled in. This means that  $-3$  is included in the solution set.

To check the answer, substitute any number greater than or equal to  $-3$  for  $x$ . Use  $x = 0$ .

$$8 + x \geq 5$$

$$8 + (0) \geq 5$$

$$8 \geq 5$$